# ПАПIBIA UПIVERSITY OF SCIEПCE AחD TECHחOLOGY 

## FACULTY OF HEALTH, NATURAL RESOURCES AND APPLIED SCIENCES SCHOOL OF NATURAL AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE

| QUALIFICATION: Bachelor of science ; Bachelor of science in Applied Mathematics and Statistics |  |
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| QUALIFICATION CODE: 07BSAM | LEVEL: 6 |
| COURSE CODE: FIM601S | COURSE NAME: FINANCIAL MATHEMATICS 2 |
| SESSION: JULY 2023 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINER | DrV. Katoma |
|  | Mrs. H.Y Nkalle |
| MODERATOR: | Prof. A.S. Eegunjobi |

## INSTRUCTIONS

- Answer ALL the questions in the booklet provided.
- Show clearly all the steps used in the calculations.
- All written work must be done in blue or black ink and sketches must be done in pencil.

PERMISSIBLE MATERIALS

- Non-programmable calculator without a cover.

THIS QUESTION PAPER CONSISTS OF 3 PAGES (Including this front page)

## Question 1 [25]

1.1 What is derivative? Mention two (2) purposes of derivatives.
[3]
1.2 Mention four (4) elements under fixed interest government borrowings.
[4]
1.3 Suppose a stock that pays no dividend is worth $N \$ 60.00$. The annual compounding interest rate is $5 \%$. What is the one-year forward price of the stock?
1.4 Consider a Put Option with a strike of $N \$ 500.00$.
(a) What would be the payoff to the buyer if the spot price at the expiration date is $N \$ 550.00$ ?
(b) What would be the payoff to the buyer if the spot price at the expiration date is N\$ 450.00?
1.5 Consider a $3 \times 9$ FRA for $£ 2000.00$ with an FRA rate of $5 \%$. Suppose the reference rate is LIBOR and the 6 -month LIBOR on the effective date is $6 \%$. Assume ACT/360 and the loan is for a period of 120 days. Find how much the borrower receives from the lender on the effective date.

## Question 2 [25]

2.1 Consider the cash-flow sequences $e=\left(e_{0}, \ldots, e_{n}\right)$ and $m=\left(m_{0}, \ldots, m_{n}\right)$. When is the cashflow " $e$ " preferable to " $m$ "?
2.2 Consider the net cash flow sequences
$\boldsymbol{A}=(50,51,-4), \boldsymbol{B}=(50,528,-22)$, at time $t=0,1,2$. Suppose the net present value for $\mathbf{A}$ is 108 and that of $\mathbf{B}$ is 594 at time 2. Find the internal rate of return for each outlay. Suppose the interest of both cash flows is $7 \%$, which one is a more viable investment?
2.3 VK Investment cc has an existing debt of $\mathbf{N} \$ 2000000$ on which it makes annual payments at an annual effective rate of LIBOR plus $0.5 \%$. VK Investment cc decides to enter a swap with a notional amount of $N \$ 2000000$ on which it makes annual payments at a fixed annual effective rate of $3 \%$ in exchange for receiving annual payments at the annual effective LIBOR rate. The annual effective LIBOR rates over the first and second years of the swap contract are $2.5 \%$ and $4 \%$ respectively. VK Investment cc does not make or receive any other payments. Calculate the net interest payment that VK Investment cc makes in the second year.
2.4 Explain the dangers of derivatives

## Question 3 [25]

3.1 Suppose a certificate of deposit is issued with a face value of $\mathrm{N} \$ 500000.00$ and a coupon of $6 \%$ for 90 days. After 30 days, its yield has fallen to $5.75 \%$. What is the price?
3.2 Consider the cash flow sequence, $a=(5,9,20,4,2), b=(6,7,3,1,36)$ at time $t=$ $0, \ldots, 4$. Find the Net Present Value (NPV) of the cash flow assuming an interest rate of $7 \%$.
3.3 Suppose a loan size of $l_{0}$ is repaid by $n m$ equal installments of size $x$ at times
$\frac{1}{m}, \frac{2}{m}, \ldots, \frac{n m}{m}=n$. Suppose the interest rate charged is $i \%$ per annum effective. Find an expression for the capital repayment for the $k^{\text {th }}$ installment.
3.4 Calculate the present value of an annuity of amount $\mathbf{N} \$ 100.00$ paid annually for 5 years at the rate of interest of $9 \%$.

## Question 4 [25]

4.1 An investment of $N \$ 200.00$ returns $N \$ 120.00$ at the end of $1^{\text {st }}$ year and $N \$ 100.00$ at the end of $2^{\text {nd }}$ year. What is the internal rate of return (IRR)?
4.2 Explain the difference between a negotiable and non-negotiable financial instrument and give an example
4.3 Frans is considering a project which requires an amount of $N \$ 3000.00$ and another amount of $N \$ 1000.00$ after one year. In two years', time, when the project ends, she expects an inflow of $N \$ 4500.00$. what is the internal rate of return (IRR) of this project? Is the above Investment profitable? Assume that Frans can lend and borrow at the same fixed rate of $7.13 \%$ per annum.
4.4 Consider the following two cash-flow sequences:

| Time (Year) | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- |
| Project A | -80 | 96 | 1 | 5 |
| Project B | -80 | 10 | 10 | 90 |

Find the Internal Rate of Return (IRR) of project A and Project B. And show that $\operatorname{IRR}(A)>$ $\operatorname{IRR}(B)$.

